Prize Problem

Let $P(x) = x^6 - x^5 - x^3 - x^2 - x$ and $Q(x) = x^4 - x^3 - x^2 - 1$ and suppose that $r_1, r_2, r_3,$ and $r_4$ are roots of $Q$. Calculate $P(r_1) + P(r_2) + P(r_3) + P(r_4)$.

Return solutions to Harris 4158 by 7 April 2017 to be eligible for prize, or submit electronic solutions to jpledford@vcu.edu.